

Structure dynamics of strongly reduced epitaxial BaTiO_{3-x} studied by Raman scattering

H.Z. Guo, Z.H. Chen*, B.L. Cheng, H.B. Lu, L.F. Liu, Y.L. Zhou

Institute of Physics and Center for Condensed Matter Physics, Chinese Academy of Sciences, P.O. Box 603, Beijing 10008, China

Available online 25 March 2005

Abstract

Raman scattering technique was used to study structure dynamics of strongly reduced epitaxial barium titanate (BaTiO_{3-x}) thin films grown on MgO (100) substrates by laser molecular beam epitaxy under different oxygen pressures from 10^{-2} to 10^{-5} Pa. X-ray diffraction and asymmetric rocking curves indicate that lattice parameters c and c/a ratio increase, and a slightly decreases with decreasing oxygen pressure, indicating increased lattice volume of BaTiO_{3-x} thin film. Raman spectra confirm that BaTiO_{3-x} thin films are in tetragonal phase with some deviated features, which maybe origin from tensile strain at film–substrate interface due to lattice parameter mismatch. Moreover, two weak peaks in Raman spectra of $\text{BaTiO}_{2.52}$ thin film grown under 3.0×10^{-5} Pa may be induced by second-order two-phonon processes. Raman peaks shift towards lower frequencies with decreasing oxygen pressure during deposition, suggesting a decrease of the stress in BaTiO_{3-x} thin films. In the meantime, Raman peaks become broadened, which may be attributed to higher degree of structural disorder in strongly reduced BaTiO_{3-x} lattice structure.

© 2005 Elsevier Ltd. All rights reserved.

Keywords: Films; Defects; Spectroscopy; Optical properties; BaTiO_3

1. Introduction

Recently, a number of studies have been focused on barium titanate (BaTiO_3) thin films due to their remarkable ferroelectric, electro-optical, high dielectric constant, and non-linear optical properties.^{1–4} To meet the need of advanced integrated electronic devices, BaTiO_3 films with small dimensions and perfect crystallinity and surface morphology are required. It has been found that the crystallinity and surface morphology of thin films can be improved by decreasing gas pressure during growth.^{5,6} Therefore, many efforts have been made to deposit BaTiO_3 films with small dimensions under low oxygen pressures. Unfortunately, it has also been revealed that dielectric and ferroelectric properties of thin films degrade with decreasing oxygen pressure due to generation of oxygen vacancies.⁷ This means that oxygen deficiency plays important roles in dielectric and ferroelectric performance. Hence, tracking the structural dynamic charac-

teristics of BaTiO_3 films as a function of deposition oxygen pressure is very important.

On the other hand, stress caused by difference of lattice mismatch and thermal expansion coefficient between thin film and substrate has always been one of the major interests in the study of ferroelectric thin films. It has been found that stress can significantly change the mechanical, dielectric and optical properties, and influence the nature of phase transitions, and enhance the dielectric constant of BaTiO_3 greatly.⁸ It is well known that Raman spectroscopy is a characterization method that measures the frequencies of the long-wavelength lattice vibrations (phonons). Unlike X-ray diffraction (XRD) or electron diffraction, Raman spectroscopy does not provide direct determination of the crystal structure, however, it has several advantages other than the diffraction methods as follows: Raman spectroscopy can give useful information about impurity, grain size, porosity and crystal symmetry of thin films.^{9,10} Furthermore, Raman scattering is greatly influenced by disorder and residual stress, which causes variation in phonon frequencies and life times, leading to broadening of Raman peaks and breakdown of Raman selection rule. The frequencies of phonons are sensitive to strains, i.e., Raman

* Corresponding author. Tel.: +86 10 82649478; fax: +86 10 82649451.
E-mail address: zhchen@aphy.iphy.ac.cn (Z.H. Chen).

peaks shift towards higher (lower) frequency are related to compressive (tensile) strains.¹¹ In the last few years, a number of groups have studied the Raman spectra of BaTiO₃ single crystals^{10,12–14} and ferroelectric single-domain crystal at room-temperature.^{15,16} However, Raman investigations of epitaxial BaTiO₃ thin films are still rare in literature.

In this paper, BaTiO_{3–x} thin films grown on single-crystal MgO (100) substrates by laser molecular-beam epitaxy (L-MBE)¹⁷ under various oxygen pressures from 10^{–2} to 10^{–5} Pa are investigated using Raman spectroscopy in combination with XRD and Rutherford backscattering spectrometry (RBS). Raman spectroscopy has been demonstrated as a powerful tool to study the structural dynamics based on effects of the oxygen deficiency and stress in ferroelectric thin films.

2. Experiments

BaTiO_{3–x} thin films were prepared on MgO (100) substrates by L-MBE using a BaTiO₃ single-crystal target. Distance from target-to-substrate was 4.5 cm. During deposition the substrate temperature was kept at 630 °C with different oxygen pressures of 3 × 10^{–2}, 3 × 10^{–3}, 3 × 10^{–4}, and 3 × 10^{–5} Pa, respectively. A Lambda Physik LEXTRA 200 excimer laser (308 nm, 28 ns) was used as the deposition light source with an energy density of about 1 J/cm² at a repetition rate of 2 Hz. The deposition rate was about 0.1 nm per pulse. In situ reflection high-energy electron diffraction (RHEED) was used to characterize the growth process of the BaTiO_{3–x} thin films. The thickness of the BaTiO_{3–x} thin films was about 300 nm.

The crystallinity and phase purity of the BaTiO_{3–x} thin films were examined by XRD with Cu Kα radiation. The oxygen pressure dependence on the crystallographic orientation and crystal parameters of BaTiO_{3–x} thin films were investigated using asymmetric rocking curve method.^{18–20} Oxygen content in the thin films was measured by RBS with an incident ⁴He⁺ (3.016 MeV in energy) ion beam, which is effective to detect oxygen.²¹ Raman scattering measurements were carried out at room temperature in backscattering geometry with a Jobin-Yvon T64000 triple Raman spectrometer. A 514.5 nm Ar⁺ ion laser line was used for excitation. Raman spectra were obtained using a microprobe device that allows the incident light to be focused on the sample with about 1–2 μm in diameter. The spectrometer provided a wave number resolution of ~0.5 cm^{–1} and accuracy of ~0.1 cm^{–1}.

3. Results and discussion

3.1. RHEED, XRD, and RBS results

A typical RHEED pattern during epitaxial growth of the BaTiO_{3–x} thin film under 3.0 × 10^{–5} Pa oxygen pressure is shown in Fig. 1. RHEED pattern indicates that the samples

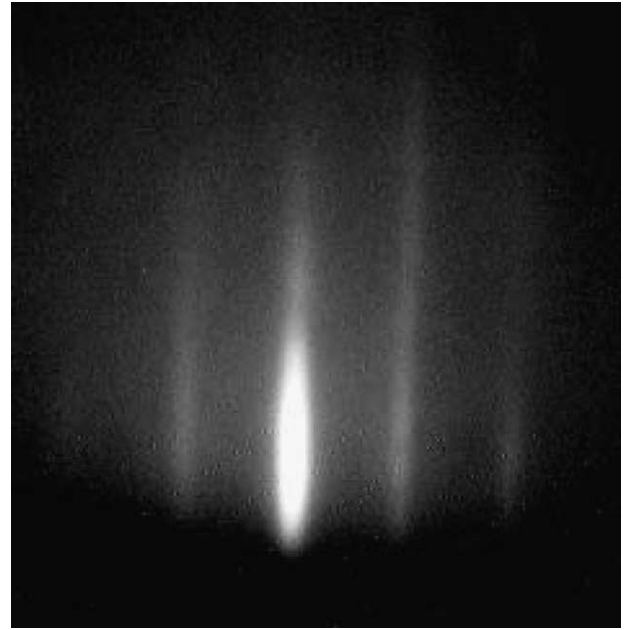


Fig. 1. Typical RHEED pattern during the epitaxial growth of the BaTiO_{3–x} thin film substrate at 670 °C under 3.0 × 10^{–5} Pa oxygen pressure.

have high crystallinity. The thickness of the BaTiO_{3–x} thin films was in situ controlled at atomic scale by monitoring of the intensity oscillation of RHEED.

A typical XRD θ – 2θ pattern of a 300-nm-thick BaTiO_{3–x} thin film grown under 3 × 10^{–5} Pa oxygen pressure on MgO substrate is shown in Fig. 2. Only (00*l*) diffraction peaks of BaTiO₃ and (100) diffraction peaks of MgO can be observed, which means that the deposited BaTiO_{3–x} thin films are single phase. The quite narrow XRD ω -rocking curves on (002) BaTiO₃, as shown by inset in Fig. 2, reveal that the BaTiO_{3–x} films are well-oriented. The full width at half-maximum (FWHM) is 0.82° for the (002) peak indicating that the films have a high degree of crystallinity. To study the relationship between the crystal structure and oxygen pressures, the asymmetric rocking curve technique is taken for

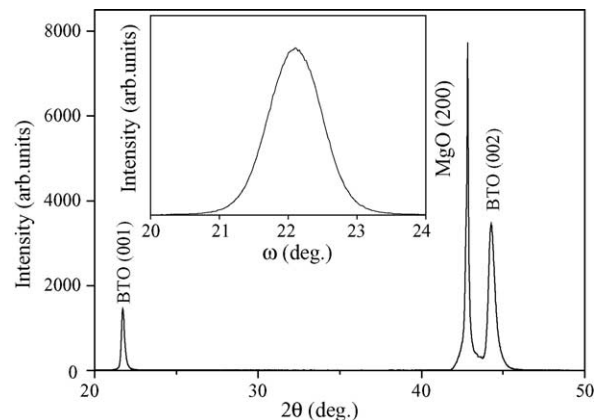


Fig. 2. XRD θ – 2θ scan of 300-nm-thick BaTiO_{3–x} thin film grown under 3.0 × 10^{–5} Pa oxygen pressure on MgO substrate. The inset shows the ω rocking curve for the (002) peak of BaTiO_{3–x} thin film.

the $\{303\}$ family of the equivalent planes in two perpendicular directions rotated 90° about the surface normal. By using XRD θ - 2θ and asymmetric ω -rocking curves, the phase and orientation of the BaTiO_{3-x} films are identified to be tetragonal with c -axis orientation.

Variations of parameters c , a and c/a ratio as a function of oxygen pressures are plotted in Fig. 3(a) and (b). The open square, open circle and open triangle represent the experimental data and the solid lines are guides to eye. As the oxygen pressure decreases, c and c/a increase while a slightly decreases, indicating that the lattice volume of the BaTiO_{3-x} thin film increases under lower oxygen pressure. This increase of lattice volume can be attributed to the effect of oxygen vacancies.^{19,22} According to the investigation on PbTiO_3 ,²² oxygen vacancies are double donor defects. The nearest two Ti^{4+} and four Pb^{2+} cations of a +2 charged oxygen vacancy are displaced away from it, while the nearest eight O^{2-} anions are attracted towards it. The displacements of Ti^{4+} and Pb^{2+} cations are along c axis and a axis, respectively. The magnitude of the displacements from ideal tetragonal positions of Ti, O, and Pb atoms are 0.021, 0.004, and 0.016 nm, respectively. Resulting from these displacements, the unit cell volume and the c/a ratio of PbTiO_3 are enlarged

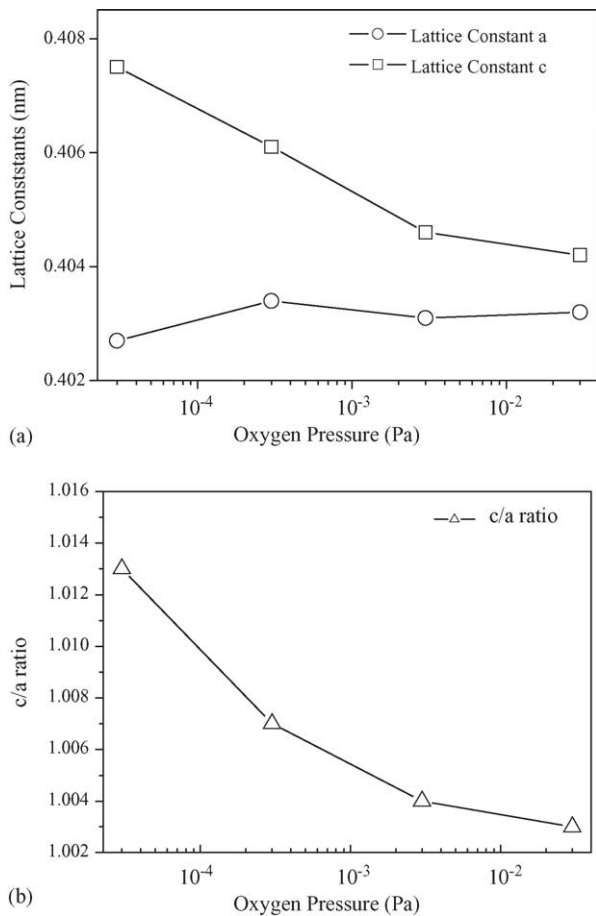


Fig. 3. (a) Lattice parameters c and a , (b) c/a ratio of BaTiO_{3-x} thin films vs. oxygen pressure.

as the oxygen pressure decreases. It is reasonable to deduce that the effect of the oxygen vacancies on the lattice structure of BaTiO_3 is similar to that of PbTiO_3 , because BaTiO_3 and PbTiO_3 belong to the same perovskite structure.

Furthermore, in order to find out how the structure of BaTiO_{3-x} thin films grown under different oxygen being different, the oxygen content in BaTiO_{3-x} thin films grown under different oxygen was analyzed by RBS as shown in Table 1. It can be seen that the stoichiometric BaTiO_3 thin film is obtained for the sample deposited under 3.0×10^{-2} Pa. As the oxygen pressure decreases, the oxygen deficiency increases. When deposited under 3.0×10^{-5} Pa, the oxygen deficiency in the BaTiO_{3-x} film is 0.48. Our results clearly show that more oxygen vacancies exist in the film grown under the oxygen pressure of 3.0×10^{-5} Pa. The results also indicate that tetragonal perovskite structure can be maintained even in the strongly reduced $\text{BaTiO}_{0.52}$ sample, which may be due to the stabilization of the tetragonality even though the large misfit tensile stress in BaTiO_{3-x} thin films.

3.2. Raman mode assignments and analyses

Single-crystal BaTiO_3 has a tetragonal structure at room temperature and has a tetragonal-cubic phase transition at its Curie temperature ($T_c = 132^\circ\text{C}$). In the cubic phase, the 12 optic modes transform as the $3F_{1u} + 1F_{2u}$ irreducible representations, and there are no first-order Raman active modes. In the tetragonal phase, each F_{1u} mode splits into one A_1 mode and one E mode, while the F_{2u} mode splits into B_1 and E , resulting in $3A_1 + B_1 + 4E$ modes. These modes further split into longitudinal (LO) and transverse (TO) components due to the long range electrostatic forces associated with lattice ionicity. Then the following distinct Raman-active optical lattice vibrations for BaTiO_3 in its tetragonal phase are obtained: $3A_1(\text{TO}) + 3A_1(\text{LO}) + 3E(\text{TO}) + 3E(\text{LO}) + 1E(\text{LO} + \text{TO}) + 1B_1$.¹² The Raman^{10–16,23} and infrared spectral²⁴ modes have been reliably identified in BaTiO_3 bulk crystal in the ferroelectric single and poly domain states. These results mentioned above will be used in the following section to compare with our results on the epitaxial film.

Fig. 4(I) and (II) show the Raman spectra of the 300-nm-thick BaTiO_{3-x} thin films on MgO substrates grown under different oxygen pressures. The centrosymmetric structure of the cubic forbids any first order Raman scattering pro-

Table 1

The chemical composition data of the BaTiO_{3-x} thin films prepared under various oxygen pressures from RBS measurements

Oxygen pressure (Pa)	Chemical composition			Oxygen deficiency x	Thickness (nm)
	Ba	Ti	O		
3.0×10^{-2}	0.96	1.00	3.00	0	300
3.0×10^{-3}	0.96	1.00	2.93	0.07	300
3.0×10^{-4}	0.94	1.00	2.82	0.18	300
3.0×10^{-5}	0.94	1.01	2.52	0.48	300

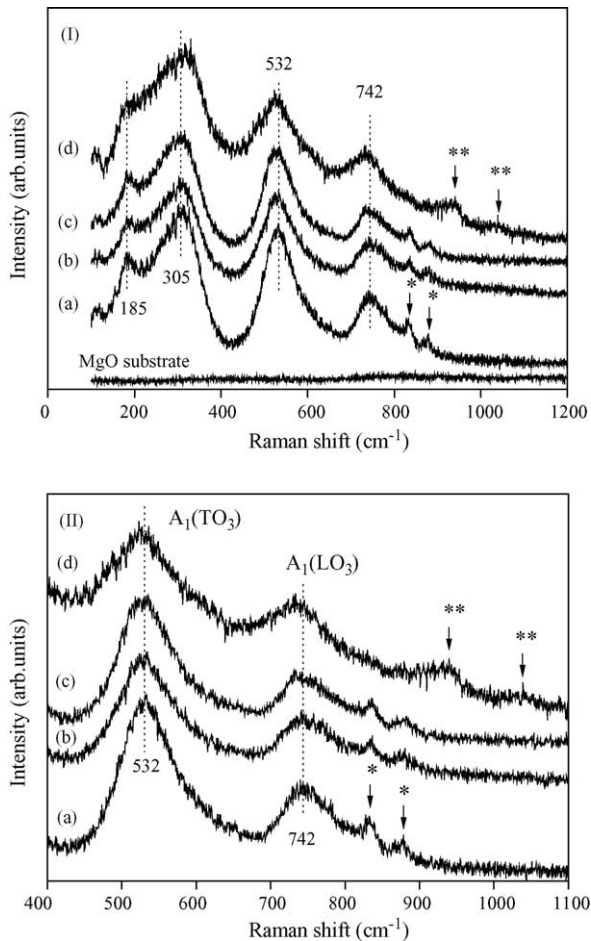


Fig. 4. (I) Raman spectra of 300-nm-thick BaTiO_{3-x} thin films on MgO substrates. BaTiO_{3-x} thin films were deposited under different oxygen pressures of (a) 3.0×10^{-2} Pa, (b) 3.0×10^{-3} Pa, (c) 3.0×10^{-4} Pa and (d) 3.0×10^{-5} Pa. Spectrum of a (100) oriented MgO substrate is also plotted here. (II) Raman spectra expanded scale.

cess. Thus, the optical phonons in bulk MgO are Raman inactive due to cubic symmetry of MgO.²⁵ Therefore, Raman scattering from the MgO substrate can be avoided and the signal from the BaTiO_{3-x} films can be confidently detected. Spectra are also re-scaled and offset for ease of comparison. Let us examine the features of the spectra in Fig. 4(I) in the order of increasing wave number. First, the interference of the $A_1(\text{TO}_1)$ mode at about $\sim 185 \text{ cm}^{-1}$ with a broad $A_1(\text{TO}_2)$ mode about 280 cm^{-1} , which is due to the coupling between A_1 modes, results in an antiresonance effect at 180 cm^{-1} . Several investigators have studied this coupling phenomenon of A_1 modes in BaTiO_3 .¹⁴ Next is the third asymmetric $A_1(\text{TO}_3)$ modes at about $\sim 532 \text{ cm}^{-1}$ that also couples weakly with the $A_1(\text{TO}_2)$ mode. The $E(\text{TO}_2)$ mode at 305 cm^{-1} mixing with the broad bands $A_1(\text{TO}_2)$ mode and the high frequency at $\sim 742 \text{ cm}^{-1}$ ($A_1(\text{LO}_3)$) are observed, which are specific to the tetragonal phase of BaTiO_3 .^{10,11} Thus the Raman spectra confirm that the BaTiO_{3-x} thin films have the tetragonal structure in agreement with the XRD results, which confirmed that the samples are *c*-axis orienta-

tion of tetragonal phase. Finally, two weak peaks at 832 and 877 cm^{-1} marked with a single asterisk in Fig. 4 maybe origin from the tensile strain at the film–substrate interface due to the lattice parameters mismatch between the BaTiO_3 single crystal and MgO (100) substrate, which were not observed by XRD measurements. Another interesting feature is the occurrence of two weak peaks at 943 and 1039 cm^{-1} marked with the double asterisks, which is only observed in the spectrum of $\text{BaTiO}_{2.52}$ thin film grown under 3.0×10^{-5} Pa. These two peaks are broad and weak, which seem to be related to the second-order two-phonon processes.²⁶ Oxygen deficiency makes the BaTiO_{3-x} lattice distorted, the more oxygen deficiencies, the more the BaTiO_{3-x} lattice distorted would be. Because of the loss of translation symmetry in the $\text{BaTiO}_{0.52}$ due to the distortion of the lattice, the phonons are not restricted to originate from a point near the Brillouin zone center. So that the phonons can originate anywhere in the Brillouin zone provided their wave vectors add up to approximately zero. This maybe account for the second-order two-phonon processes in the strongly reduced $\text{BaTiO}_{0.52}$ thin film.

It can be observed from Fig. 4(I) and (II) that all the Raman modes observed in these BaTiO_{3-x} thin films are found at higher frequencies (blue shift) than the corresponding modes in the BaTiO_3 single crystal.^{10,12–14} Moreover, the Raman spectra also show that the blue shifts of the Raman modes become smaller and smaller with decreasing oxygen pressure. Meanwhile, Raman scattering results, displayed in Fig. 4(I) and (II), show that the peaks decrease in intensity with decreasing oxygen pressure during deposition, and the bands broaden more and more. We used Lorentzian functions to fit the $A_1(\text{TO}_3)$ and $A_1(\text{LO}_3)$ peaks. The corresponding results of the Raman shift and peak width as a function of the oxygen pressure are plotted in Fig. 5. It is found that the $A_1(\text{TO}_3)$ and $A_1(\text{LO}_3)$ peaks shift to lower frequency, but the peak width increases continuously with decreasing oxygen pressure.

The observed broadening of the Raman peaks maybe arises from the coupling of the normal modes with the static

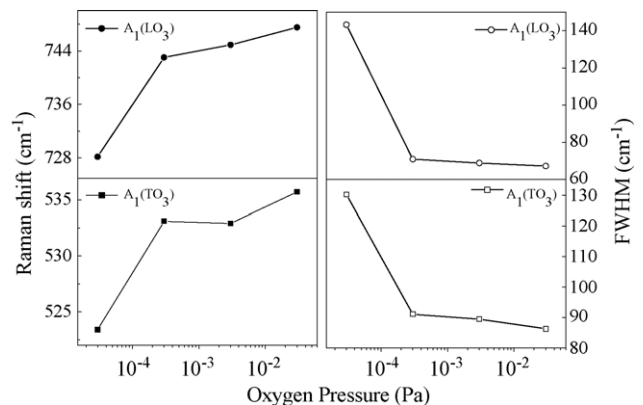


Fig. 5. Oxygen pressure dependences of Raman shift and peak width for the $A_1(\text{TO}_3)$ and $A_1(\text{LO}_3)$ modes.

distortion.²⁷ The distortion of the lattice leads to the breakdown of the translation symmetry, thus the $q=0$ Raman selection rules are relaxed. The phonon frequencies also shift remarkably towards higher/lower value, depending upon the tensile/compressive nature of the stresses.¹¹ The blue shifts of the Raman modes are the characteristic of the presence of the tensile stresses in our samples. Chen et al.²⁸ have also found the presence of the tensile stresses in the Ce doped BaTiO₃ thin films on MgO substrates. Furthermore, the Grüneisen law: $\Delta\nu/\nu = -\gamma\Delta V/V$, provides a good approximation for the frequency shift due to lattice enlarged.²⁹ Where ν is the Raman frequency, V is the unit cell volume, and γ is the Grüneisen parameter. At lower oxygen pressure, the density of oxygen vacancies is higher, and then the expansion of the lattice volume is greater. Then the Raman modes shift to lower frequencies (see Fig. 4). Meanwhile, the lattice mismatch between BaTiO_{3-x} thin films and MgO substrate becomes smaller, indicating the releasing of the residual stresses occurred through oxygen vacancies generation. Moreover, oxygen deficiency makes the BaTiO_{3-x} lattice distorted, which further make the broadening of the peaks and appearances of new Raman peaks.

4. Conclusion

In conclusion, a series of highly *c*-axis oriented strongly reduced epitaxial BaTiO_{3-x} thin films were epitaxially grown with different oxygen pressures from 3.0×10^{-2} to 3.0×10^{-5} Pa on the MgO substrates by L-MBE. A relationship between the structural parameters and the density of oxygen vacancies of the samples were systematically investigated. The results indicate that, with decreasing oxygen pressure during deposition, the oxygen deficiency and the cell unit volume increase increases, while the perovskite structure can be maintained in strongly reduced BaTiO_{3-x} with the oxygen deficiency being as high as 0.48. Furthermore, the structure dynamics in the samples, such as stress effect, oxygen defects, structural disorder, etc., depending on oxygen deficiency have been investigated by means of Raman scattering. The results indicate that, with decreasing oxygen pressure during deposition, the stress in BaTiO_{3-x} thin films becomes smaller; in the meantime the structural disorder becomes larger. In addition, two weak peaks at 943 and 1039 cm⁻¹ in strongly reduced BaTiO_{2.52} thin film seem to be related to the second-order two-phonon processes.

Acknowledgments

The authors would like to thank Yulong Liu and Ke Zhu for their helps in Raman scattering measurements and for many fruitful discussions. The work was financially supported by the National Natural Science Foundation of China.

References

1. Sayer, M. and Sreenivas, K., Ceramic thin films: fabrication and applications. *Science*, 1990, **247**, 1056–1060.
2. Cohen, R. E., Origin of ferroelectricity in perovskite oxides. *Nature*, 1992, **358**, 136–138.
3. Lee, M. B., Kawasaki, M., Yoshimoto, M. and Koinuma, H., Heteroepitaxial growth of BaTiO₃ films on Si by pulsed laser deposition. *Appl. Phys. Lett.*, 1995, **66**, 1331–1333.
4. Roy, D. and Krupanidhi, S. B., Pulsed excimer laser ablated barium titanate thin films. *Appl. Phys. Lett.*, 1992, **61**, 2057–2059.
5. Shigetani, H., Kobayashi, K., Fujimoto, M., Sugimura, W., Matsui, Y. and Tanaka, J., BaTiO₃ thin films grown on SrTiO₃ substrates by a molecular-beam-epitaxy method using oxygen radicals. *J. Appl. Phys.*, 1997, **81**, 693–697.
6. Yoneda, Y., Okabe, T., Sakaue, K., Terauchi, H., Kasatani, H. and Deguchi, K., Structural characterization of BaTiO₃ thin films grown by molecular beam epitaxy. *J. Appl. Phys.*, 1998, **83**, 2458–2461.
7. Fukuda, Y., Haneda, H., Sakaguchi, I., Nuwata, K., Aoki, K. and Nishimura, A., Dielectric properties of (Ba, Sr)TiO₃ thin films and their correlation with oxygen vacancy density. *Jpn. J. Appl. Phys. Part 1*, 1997, **36**, L1514–L1516.
8. Yano, Y., Iijima, K., Daitoh, Y., Terashima, T., Bando, Y., Watanabe, Y. et al., Epitaxial growth and dielectric properties of BaTiO₃ films on Pt electrodes by reactive evaporation. *J. Appl. Phys.*, 1994, **76**, 7833–7838.
9. Siu, G. G., Stokes, M. J. and Liu, Y. L., Variation of fundamental and higher-order Raman spectra of ZrO₂ nanograins with annealing temperature. *Phys. Rev. B*, 1999, **59**, 3173–3179.
10. Robins, L. H., Kaiser, D., Rotter, L. D., Schenck, P. K., Stauff, G. T. and Rytz, D., Investigation of the structure of barium titanate thin films by Raman spectroscopy. *J. Appl. Phys.*, 1994, **76**, 7487–7498.
11. Wickboldt, P., Anastassakis, E., Sauer, R. and Cardona, M., Raman phonon piezospectroscopy in GaAs: infrared measurements. *Phys. Rev. B*, 1987, **35**, 1362–1368.
12. DiDomenico, M., Wemple, S. H., Porto, S. P. S. and Bauman, R. P., Raman spectrum of single-domain BaTiO₃. *Phys. Rev.*, 1968, **174**, 522–530.
13. Wang, R. P., Jiang, Y. J., Zeng, L. Z., Liu, Y. L. and Zhu, Y., Dispersion of the oblique phonons in tetragonal BaTiO₃ and Ce:BaTiO₃. *J. Raman Spectrosc.*, 1995, **26**, 295–299.
14. Chaves, A., Katiyar, R. S. and Porto, S. P. S., Coupled modes with A₁ symmetry in tetragonal BaTiO₃. *Phys. Rev. B*, 1974, **10**, 3522–3533.
15. Tarrach, G., Lagos, L. P. and Hermans, Z. R., Nanometer spot allocation for Raman spectroscopy on ferroelectrics by polarization and piezoresponse force microscopy. *Appl. Phys. Lett.*, 2001, **79**, 3152–3154.
16. Jiang, Y. J., Zeng, L. Z., Wang, R. P., Zhu, Y. and Liu, Y. L., Fundamental and second-order Raman spectra of BaTiO₃. *J. Raman Spectrosc.*, 1996, **27**, 31–34.
17. Cui, D. F., Lu, H. B., Wang, H. S., Chen, Z. H., Zhou, Y. L., Yang, G. Z. et al., Atomic force microscopy studies of barium titanate thin films prepared by laser molecular beam epitaxy. *Chin. Phys. Lett.*, 1997, **14**, 134–137.
18. Li, C. L., Cui, D. F., Zhou, Y. L., Lu, H. B., Chen, Z. H., Zhang, D. F. et al., Asymmetric rocking curve study of the crystal structure orientations for BaTiO₃ thin films grown by pulsed laser deposition. *Appl. Surf. Sci.*, 1998, **136**, 173–177.
19. Zhao, T., Chen, F., Lu, H. B., Yang, G. Z. and Chen, Z. H., Thickness and oxygen pressure dependent structural characteristics of BaTiO₃ thin films grown by laser molecular beam epitaxy. *J. Appl. Phys.*, 2000, **87**, 7442–7447.
20. Kang, M. H., Ku, J. K. and Baik, S., Crystallographic characterization of tetragonal (Pb,Lu)TiO₃ epitaxial thin films grown by pulsed laser deposition. *J. Appl. Phys.*, 1995, **78**, 2601–2606.
21. Cheng, H. S., Shen, H., Tang, J. Y. and Yang, F. J., Cross sections for 170° backscattering of ⁴He from oxygen in the energy range

- of 2.0–9.0 MeV. *Nucl. Instrum. Methods Phys. Res. B*, 1993, **83**, 449–453.
22. Park, C. H. and Chadi, D. J., Microscopic study of oxygen-vacancy defects in ferroelectric perovskites. *Phys. Rev. B*, 1998, **57**, R13961–R13964.
23. Kim, T. W., Jung, M. and Kim, H. J., Structural and electrical properties of BaTiO₃ thin films grown on *p*-InSb substrate by metalorganic chemical vapor deposition at low temperature. *Appl. Phys. Lett.*, 1994, **62**, 1788–1790.
24. Sanjurjo, J. A., Katiyar, R. S. and Porto, S. P. S., Temperature dependence of dipolar modes in ferroelectric BaTiO₃ by infrared studies. *Phys. Rev. B*, 1980, **22**, 2396–2403.
25. Yuzyuk, Y. E., Alyoshin, V. A., Zakharchenko, I. N., Sviridov, E. V., Almeida, A. and Chaves, M. R., Polarization-dependent Raman spectra of heteroepitaxial (Ba,Sr)TiO₃/MgO thin films. *Phys. Rev. B*, 2002, **65**, 134107.
26. Hayes, W. and Loudon, R., *Scattering of Light by Crystals*. John Wiley and Sons, New York, 1978, pp. 121–131.
27. Uwe, H., Lyons, K. B., Carter, H. L. and Fleury, P. A., Ferroelectric microregions and Raman scattering in KTaO₃. *Phys. Rev. B*, 1986, **33**, 6436.
28. Chen, M. S., Shen, Z. X., Tang, S. H., Shi, W. S., Cui, D. F. and Chen, Z. H., Stress effect on Raman spectra of Ce-doped BaTiO₃ films. *J. Phys. Condens. Matter*, 2000, **12**, 7013–7023.
29. Granado, E., Garcia, A., Sanjurjo, J. A., Rettori, C., Torriani, I., Prado, F. et al., Magnetic ordering effects in the Raman spectra of La_{1-x}Mn_{1-x}O₃. *Phys. Rev. B*, 1999, **60**, 11879–11882.